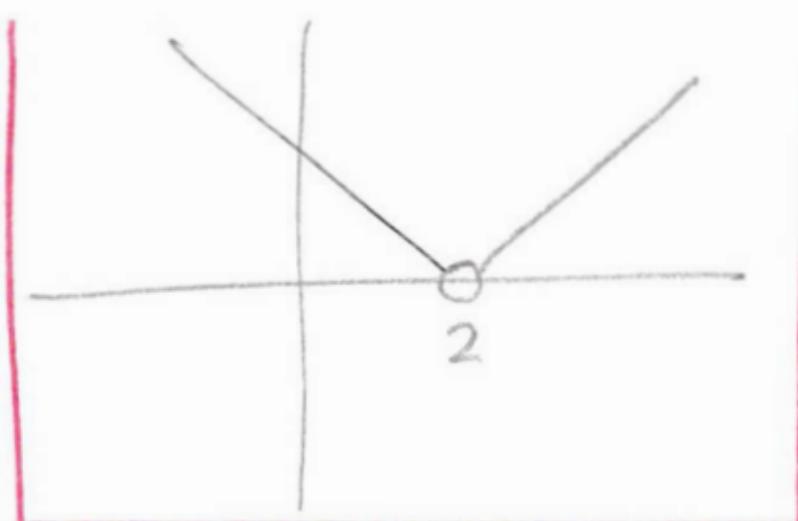


[2]

BG IS WRONG, BECAUSE  $f$  MIGHT NOT BE CONTINUOUS

AT  $x=2$



[3] DOMAIN OF  $f$  IS  $x > 0$  AND  $1 + \ln x \neq 0$   
 ( $\ln x$  DNE IF  $x \leq 0$ )

$$\ln x \neq -1$$

$$x \neq e^{-1} \text{ or } \frac{1}{e} \approx \frac{1}{3}$$

DISCONTINUOUS ON  $(-\infty, 0]$  AND AT  $x = \frac{1}{e}$

$f(0)$  DNE  $\rightarrow$  NO  $y$ -INT

$$\frac{1}{1 + \ln x} = 0 \rightarrow \text{NO SOLN} \rightarrow \text{NO } x\text{-INT}$$

$$\lim_{x \rightarrow 0^+} \frac{1}{1 + \ln x} = 0$$

$$\frac{1}{1 - \infty} \rightarrow \frac{1}{-\infty}$$

$$\lim_{x \rightarrow \frac{1}{e}^+} \frac{1}{1 + \ln x} = \infty$$

$$\lim_{x \rightarrow \frac{1}{e}^-} \frac{1}{1 + \ln x} = -\infty$$

V.A. @  $x = \frac{1}{e}$

$$\frac{1}{1 + (-1)^+} \rightarrow \frac{1}{0^+}$$

$$\frac{1}{1 + (-1)^-} \rightarrow \frac{1}{0^-}$$

$$\lim_{x \rightarrow \infty} \frac{1}{1 + \ln x} = 0$$

$\lim_{x \rightarrow -\infty} \frac{1}{1 + \ln x}$  DNE SINCE DOMAIN

$$\frac{1}{1 + \infty} \rightarrow \frac{1}{\infty}$$

H.A. @  $y = 0$  EXCLUDES  $x < 0$

$$f(x) = (1 + \ln x)^{-1}$$

$$f'(x) = -x^{-1}(1 + \ln x)^{-2} \text{ DNE @ } x \leq 0 \text{ AND } x = \frac{1}{e}$$

NOT IN DOMAIN

$$= -\frac{1}{x(1 + \ln x)^2} \text{ IS NEVER } 0 \rightarrow \text{NO CRITICAL NUMBERS}$$

$$f''(x) = x^{-2}(1 + \ln x)^{-2} + 2x^{-1}x^{-1}(1 + \ln x)^{-3}$$

$$= x^{-2}(1 + \ln x)^{-3}(1 + \ln x + 2)$$

$$= x^{-2}(1 + \ln x)^{-3}(3 + \ln x) \text{ DNE @ } x \leq 0 \text{ AND } x = \frac{1}{e}$$

NOT IN DOMAIN

$$= \frac{3 + \ln x}{x^2(1 + \ln x)^3} = 0 \quad @ \quad \begin{aligned} 3 + \ln x &= 0 \\ \ln x &= -3 \end{aligned}$$

$$f(e^{-3}) = \frac{1}{1 + \ln e^{-3}} = \frac{1}{1 - 3} = -\frac{1}{2} \quad x = e^{-3} = \frac{1}{e^3} \approx \frac{1}{27}$$

$$\lim_{x \rightarrow 0^+} -x^{-1}(1+\ln x)^2 = \lim_{x \rightarrow 0^+} \frac{-x^{-1}}{(1+\ln x)^2} = \lim_{x \rightarrow 0^+} \frac{x^{-2}}{2(1+\ln x)x^{-1}}$$

$$-\infty \cdot (1-\infty)^2 \rightarrow -\infty \cdot (\infty)^2 \rightarrow -\infty \cdot 0$$

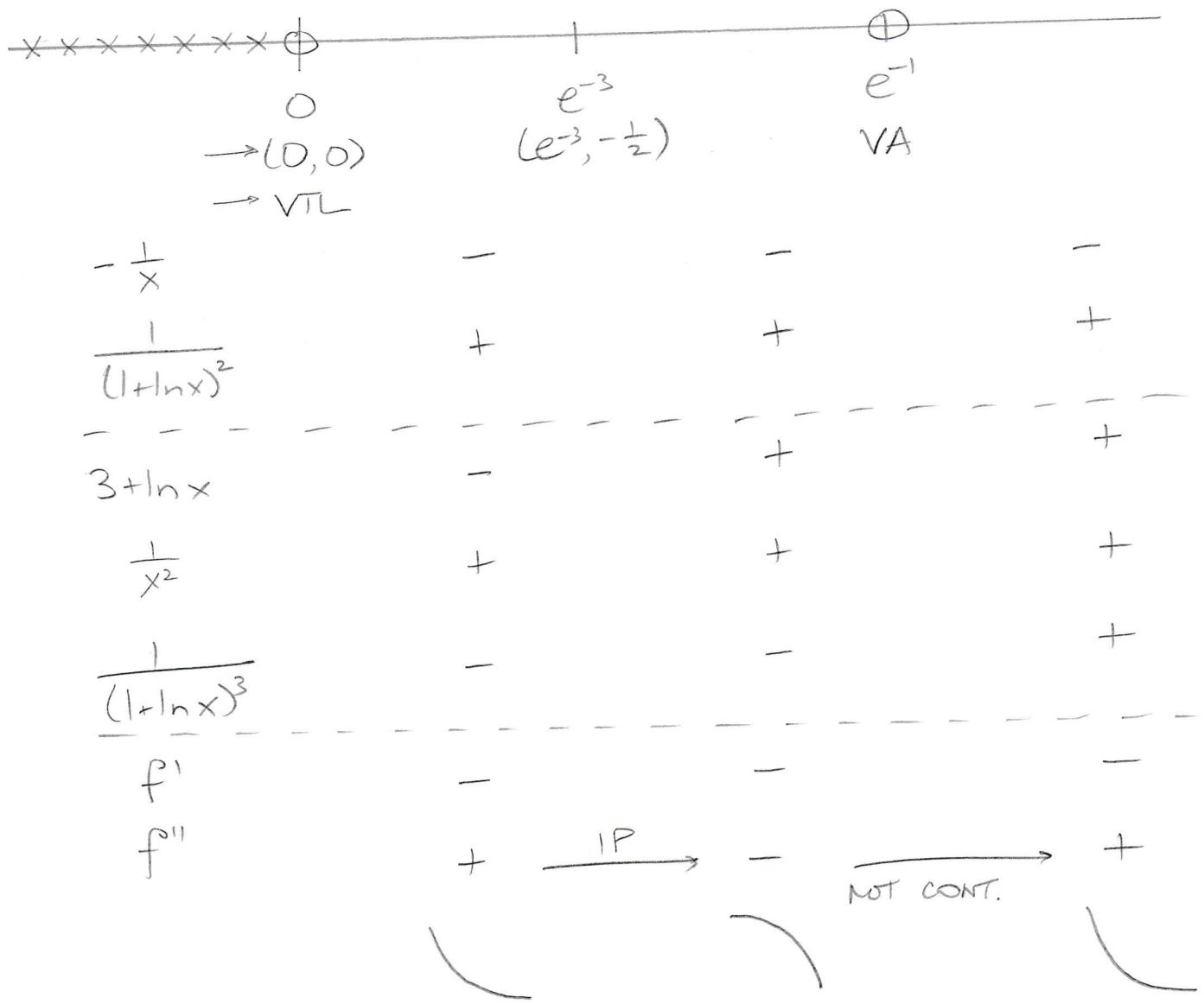
$$= \lim_{x \rightarrow 0^+} \frac{x^{-1}}{2(1+\ln x)} \quad \frac{\infty}{-\infty}$$

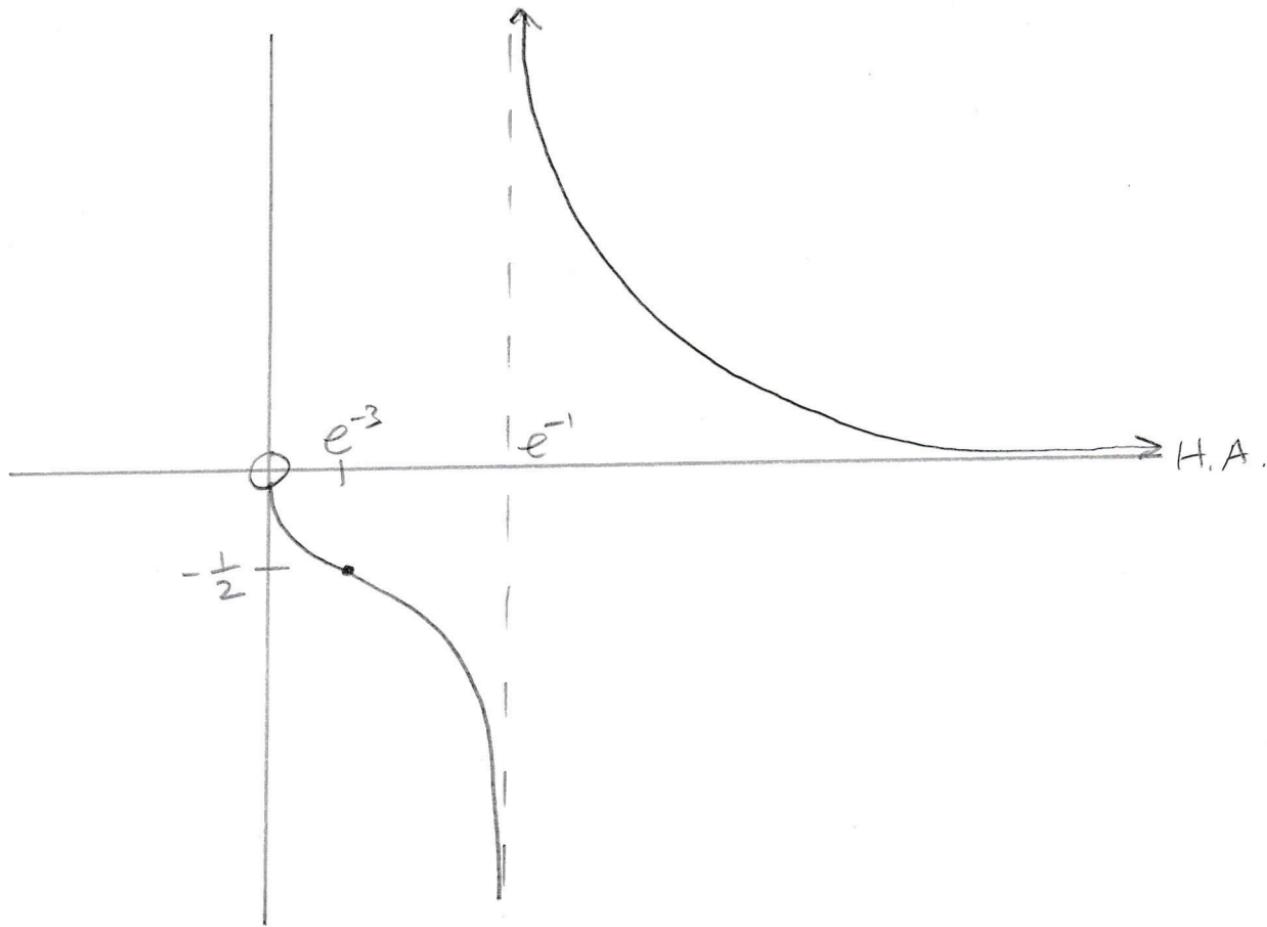
$$= \lim_{x \rightarrow 0^+} \frac{-x^{-2}}{2x^{-1}}$$

$$= \lim_{x \rightarrow 0^+} -\frac{1}{2x} = -\infty$$

$$-\frac{1}{0^+}$$

APPROACHING VTL AS  $x \rightarrow 0^+$





[4] B6 IS WRONG, BECAUSE  $f''$  MIGHT NOT CHANGE SIGNS  
AT  $x=2$

$$f(x) = (x-2)^4$$

$$f'(x) = 4(x-2)^3$$

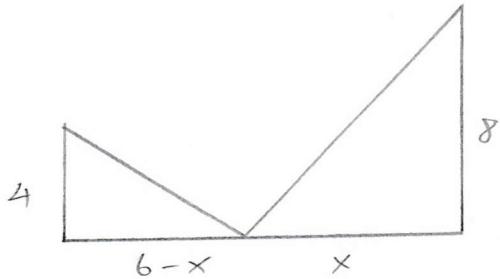
$$f''(x) = 12(x-2)^2 \rightarrow f''(2) = 0 \text{ BUT } f''(x) > 0 \text{ FOR ALL } x \neq 2$$

so  $f$  IS CONCAVE UP

ON  $(-\infty, \infty)$

IE. NO CHANGE IN  
CONCAVITY, SO NO  
INFLECTION POINTS

[5]



$$\text{MINIMIZE } d = \sqrt{x^2 + 64} + \sqrt{(6-x)^2 + 16}$$

$$x \in [0, 6]$$

$$d' = \left[ \frac{1}{2}(x^2 + 64)^{-\frac{1}{2}}(2x) + \frac{1}{2}((6-x)^2 + 16)^{\frac{1}{2}}2(6-x)(-1) \right]$$

$$= \left[ \frac{x}{\sqrt{x^2 + 64}} - \frac{6-x}{\sqrt{(6-x)^2 + 16}} \right] \text{ EXISTS ON } [0, 6]$$

(BOTH RADICANDS  
ARE POSITIVE)

$$\frac{x}{\sqrt{x^2 + 64}} - \frac{6-x}{\sqrt{(6-x)^2 + 16}} = 0$$

$$\frac{x}{\sqrt{x^2 + 64}} = \frac{6-x}{\sqrt{(6-x)^2 + 16}}$$

$$\frac{x^2}{x^2 + 64} = \frac{(6-x)^2}{(6-x)^2 + 16}$$

$$x^2(6-x)^2 + 16x^2 = \cancel{x^2(6-x)^2} + 64(6-x)^2$$

$$x^2 = 4(6-x)^2$$

$$\pm x = 2(6-x)$$

$$x = 12 - 2x \text{ or } -x = 12 - 2x$$

$$3x = 12$$

$$x = 4$$

$$\cancel{x = 12}$$

NOT IN  $[0, 6]$

$$\begin{aligned} d(0) &= \sqrt{64} + \sqrt{52} \\ &= 8 + 2\sqrt{13} > 14 \end{aligned}$$

$$\begin{aligned} d(4) &= \sqrt{80} + \sqrt{20} \\ &= 4\sqrt{5} + 2\sqrt{5} \\ &= 6\sqrt{5} = \sqrt{180} \end{aligned}$$

$$\begin{aligned} d(6) &= \sqrt{100} + \sqrt{16} \\ &= 14 = \sqrt{196} \end{aligned}$$

$d(4)$  IS MINIMUM

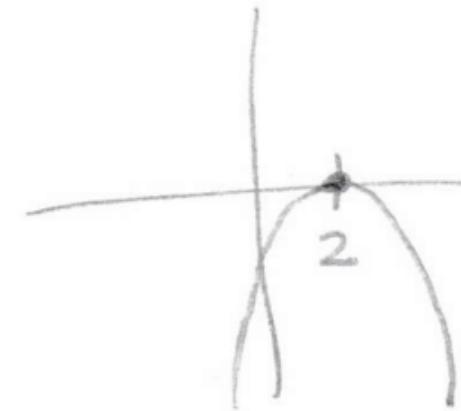
YOU SHOULD WALK  
TO THE POINT ON THE  
ROAD 200 FT DOWN  
THE ROAD FROM CG'S  
HOUSE

[6] B6 IS WRONG

$$f(x) = -(x-2)^4$$

$$f'(x) = -4(x-2)^3$$

$$f''(x) = -12(x-2)^2$$



$f$  IS CONT + DIFF ON  $(-\infty, \infty)$  SINCE  $f$  IS POLYNOMIAL

BUT  $f''(2) = 0$

$$[7] \quad \lim_{\substack{\text{im} \\ x \rightarrow 0^+}} \frac{2x - 1 + \sec^2 x}{4x^3 - 6x^2} = \lim_{\substack{\text{im} \\ x \rightarrow 0^+}} \frac{2 + 2\sec^2 x \tan x}{12x^2 - 12x} = \lim_{\substack{x \rightarrow 0^+ \\ x \neq -1}} \frac{2 + 2\sec^2 x \tan x}{12x(x-1)}$$

$$\frac{0-1+1}{0-0} \rightarrow \frac{0}{0}$$

$$\frac{2+0}{0-0} \rightarrow \frac{2}{0} = -\infty$$